lab3

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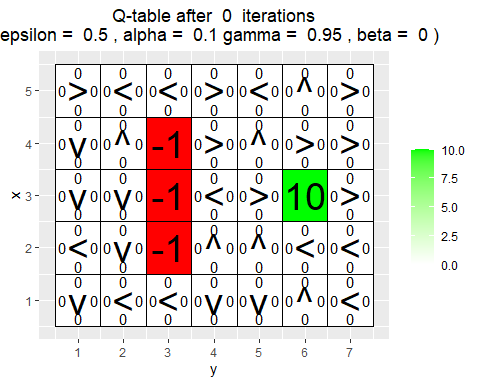
arrows <- c("^", ">", "v", "<")  
action\_deltas <- list(c(1,0), # up  
 c(0,1), # right  
 c(-1,0), # down  
 c(0,-1)) # left

vis\_environment <- function(iterations=0, epsilon = 0.5, alpha = 0.1, gamma = 0.95, beta = 0){  
   
 # Visualize an environment with rewards.   
 # Q-values for all actions are displayed on the edges of each tile.  
 # The (greedy) policy for each state is also displayed.  
 #   
 # Args:  
 # iterations, epsilon, alpha, gamma, beta (optional): for the figure title.  
 # reward\_map (global variable): a HxW array containing the reward given at each state.  
 # q\_table (global variable): a HxWx4 array containing Q-values for each state-action pair.  
 # H, W (global variables): environment dimensions.  
   
 df <- expand.grid(x=1:H,y=1:W)  
 foo <- mapply(function(x,y) ifelse(reward\_map[x,y] == 0,q\_table[x,y,1],NA),df$x,df$y)  
 df$val1 <- as.vector(round(foo, 2))  
 foo <- mapply(function(x,y) ifelse(reward\_map[x,y] == 0,q\_table[x,y,2],NA),df$x,df$y)  
 df$val2 <- as.vector(round(foo, 2))  
 foo <- mapply(function(x,y) ifelse(reward\_map[x,y] == 0,q\_table[x,y,3],NA),df$x,df$y)  
 df$val3 <- as.vector(round(foo, 2))  
 foo <- mapply(function(x,y) ifelse(reward\_map[x,y] == 0,q\_table[x,y,4],NA),df$x,df$y)  
 df$val4 <- as.vector(round(foo, 2))  
 foo <- mapply(function(x,y)   
 ifelse(reward\_map[x,y] == 0,arrows[GreedyPolicy(x,y)],reward\_map[x,y]),df$x,df$y)  
 df$val5 <- as.vector(foo)  
 foo <- mapply(function(x,y) ifelse(reward\_map[x,y] == 0,max(q\_table[x,y,]),  
 ifelse(reward\_map[x,y]<0,NA,reward\_map[x,y])),df$x,df$y)  
 df$val6 <- as.vector(foo)  
   
 print(ggplot(df,aes(x = y,y = x)) +  
 scale\_fill\_gradient(low = "white", high = "green", na.value = "red", name = "") +  
 geom\_tile(aes(fill=val6)) +  
 geom\_text(aes(label = val1),size = 4,nudge\_y = .35,na.rm = TRUE) +  
 geom\_text(aes(label = val2),size = 4,nudge\_x = .35,na.rm = TRUE) +  
 geom\_text(aes(label = val3),size = 4,nudge\_y = -.35,na.rm = TRUE) +  
 geom\_text(aes(label = val4),size = 4,nudge\_x = -.35,na.rm = TRUE) +  
 geom\_text(aes(label = val5),size = 10) +  
 geom\_tile(fill = 'transparent', colour = 'black') +   
 ggtitle(paste("Q-table after ",iterations," iterations\n",  
 "(epsilon = ",epsilon,", alpha = ",alpha,"gamma = ",gamma,", beta = ",beta,")")) +  
 theme(plot.title = element\_text(hjust = 0.5)) +  
 scale\_x\_continuous(breaks = c(1:W),labels = c(1:W)) +  
 scale\_y\_continuous(breaks = c(1:H),labels = c(1:H)))  
   
}  
  
GreedyPolicy <- function(x, y){  
   
 # Get a greedy action for state (x,y) from q\_table.  
 #  
 # Args:  
 # x, y: state coordinates.  
 # q\_table (global variable): a HxWx4 array containing Q-values for each state-action pair.  
 #   
 # Returns:  
 # An action, i.e. integer in {1,2,3,4}.  
   
 # Your code here.  
   
 maxVal <- which(q\_table[x, y, ] == max(q\_table[x, y, ]))  
 if(length(maxVal) > 1){  
 return(sample(maxVal, 1))  
 } else {  
 return(maxVal)  
 }  
   
}  
  
EpsilonGreedyPolicy <- function(x, y, epsilon){  
   
 # Get an epsilon-greedy action for state (x,y) from q\_table.  
 #  
 # Args:  
 # x, y: state coordinates.  
 # epsilon: probability of acting randomly.  
 #   
 # Returns:  
 # An action, i.e. integer in {1,2,3,4}.  
   
 # Your code here.  
   
 randomDraw <- runif(1, 0, 1)  
 maxVal <- GreedyPolicy(x, y)  
 if(randomDraw <= 1 - epsilon){  
 return(maxVal)  
 } else {  
 return(sample(1:4,1))  
 }  
   
}  
  
transition\_model <- function(x, y, action, beta){  
   
 # Computes the new state after given action is taken. The agent will follow the action   
 # with probability (1-beta) and slip to the right or left with probability beta/2 each.  
 #   
 # Args:  
 # x, y: state coordinates.  
 # action: which action the agent takes (in {1,2,3,4}).  
 # beta: probability of the agent slipping to the side when trying to move.  
 # H, W (global variables): environment dimensions.  
 #   
 # Returns:  
 # The new state after the action has been taken.  
   
 delta <- sample(-1:1, size = 1, prob = c(0.5\*beta,1-beta,0.5\*beta))  
 final\_action <- ((action + delta + 3) %% 4) + 1  
 foo <- c(x,y) + unlist(action\_deltas[final\_action])  
 foo <- pmax(c(1,1),pmin(foo,c(H,W)))  
   
 return (foo)  
}  
  
q\_learning <- function(start\_state, epsilon = 0.5, alpha = 0.1, gamma = 0.95,   
 beta = 0){  
   
 # Perform one episode of Q-learning. The agent should move around in the   
 # environment using the given transition model and update the Q-table.  
 # The episode ends when the agent reaches a terminal state.  
 #   
 # Args:  
 # start\_state: array with two entries, describing the starting position of the agent.  
 # epsilon (optional): probability of acting greedily.  
 # alpha (optional): learning rate.  
 # gamma (optional): discount factor.  
 # beta (optional): slipping factor.  
 # reward\_map (global variable): a HxW array containing the reward given at each state.  
 # q\_table (global variable): a HxWx4 array containing Q-values for each state-action pair.  
 #   
 # Returns:  
 # reward: reward received in the episode.  
 # correction: sum of the temporal difference correction terms over the episode.  
 # q\_table (global variable): Recall that R passes arguments by value. So, q\_table being  
 # a global variable can be modified with the superassigment operator <<-.  
   
 # Your code here.  
   
 curr\_state <- start\_state  
 episode\_correction <- 0  
   
 repeat{  
 # Follow policy, execute action, get reward.  
 x <- curr\_state[1]  
 y <- curr\_state[2]  
   
 action <- EpsilonGreedyPolicy(x, y, epsilon)  
   
 next\_state <- transition\_model(x, y, action, beta)  
   
 next\_x <- next\_state[1]  
 next\_y <- next\_state[2]  
   
 reward <- reward\_map[next\_x, next\_y]  
   
 # Q-table update.  
   
 tmp\_ep\_diff <- reward + gamma \* max(q\_table[next\_x, next\_y, ]) - q\_table[x, y, action]  
   
 episode\_correction <- episode\_correction + tmp\_ep\_diff  
   
 q\_table[x, y, action] <<- q\_table[x, y, action] + alpha \* tmp\_ep\_diff  
   
 if(reward!=0){  
 # End episode.  
 return (c(reward,episode\_correction))  
 }  
 curr\_state <- next\_state  
 }  
   
}

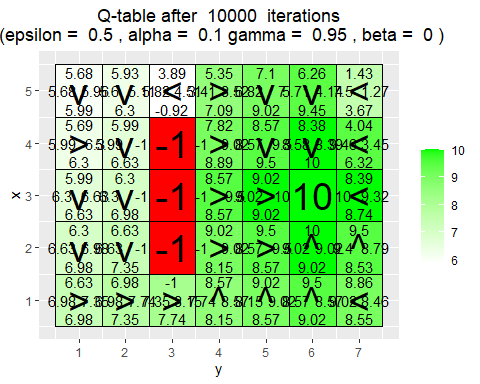
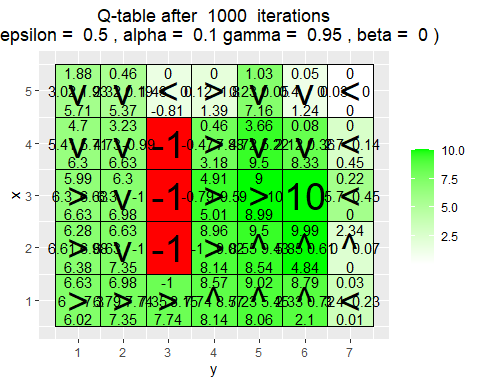
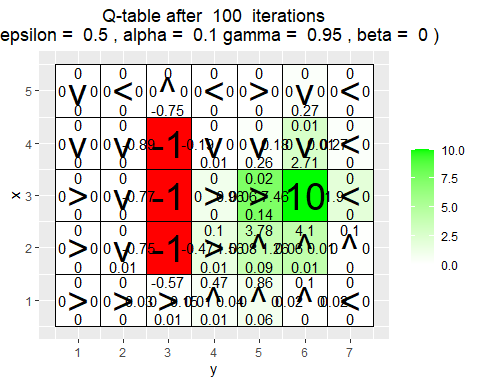
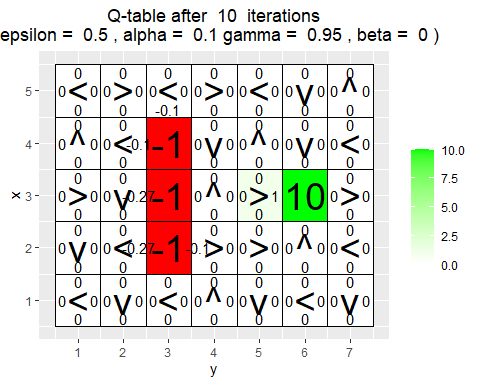
## Q-Learning Environments

## Environment A (learning)

H <- 5  
W <- 7  
  
reward\_map <- matrix(0, nrow = H, ncol = W)  
reward\_map[3,6] <- 10  
reward\_map[2:4,3] <- -1  
  
q\_table <- array(0,dim = c(H,W,4))  
  
vis\_environment()



for(i in 1:10000){  
 foo <- q\_learning(start\_state = c(3,1))  
   
 if(any(i==c(10,100,1000,10000)))  
 vis\_environment(i)  
}



* What has the agent learned after the first 10 episodes ?

Almost nothing, it has found that moving in to the -1 states are bad but it did not learn to move towards the +10 state.

* Is the final greedy policy (after 10000 episodes) optimal for all states, i.e. not only for the initial state ? Why / Why not ?

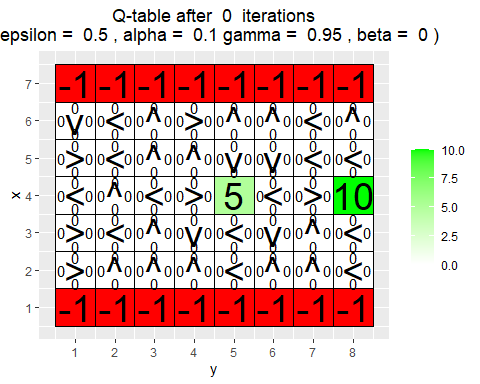
No it is not, an optimal policy would be to always move to the +10 state in thew shortest possible way. We can see some states where this is not the case, for example in the corner where x,y = 1,1 and the neighboring states. The optimal route would be to go underneath the -1 block but it instead goes up and over.

* Do the learned values in the Q-table reflect the fact that there are multiple paths (above and below the negative rewards) to get to the positive reward ? If not, what could be done to make it happen ?

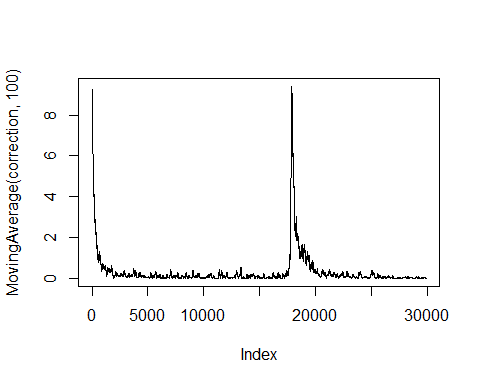
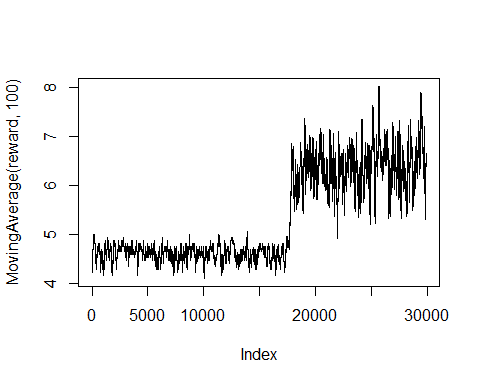
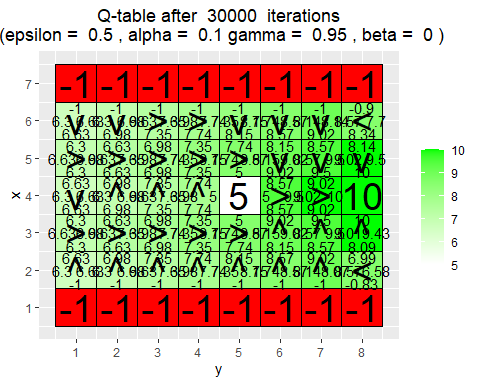
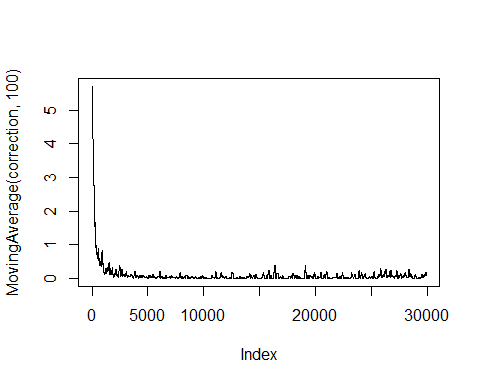
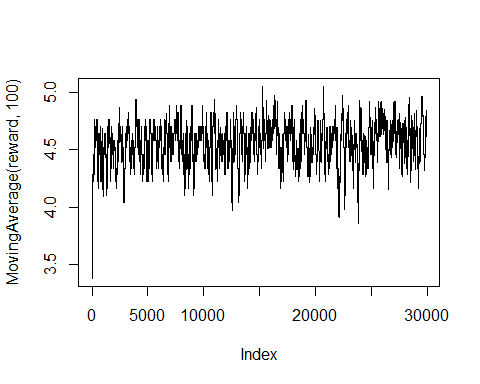
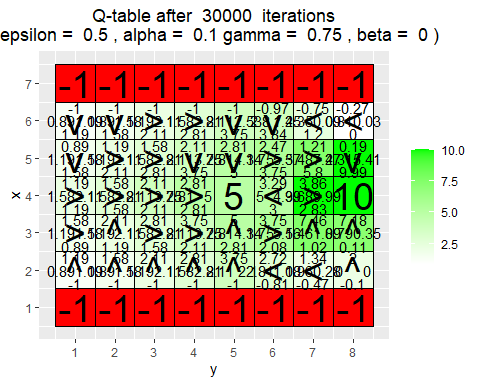
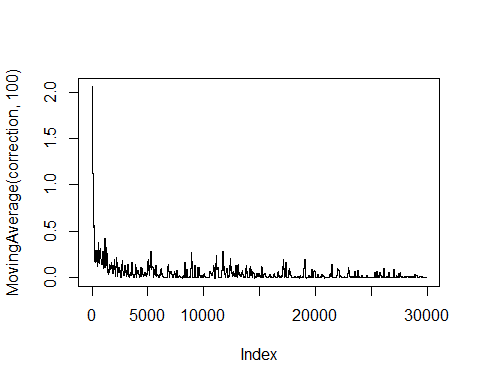
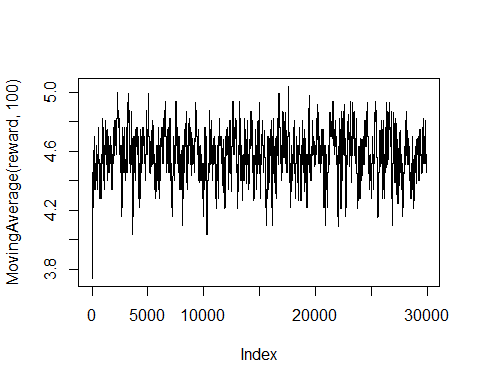
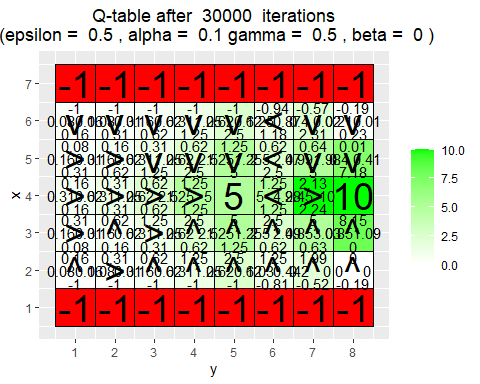
No, as stated in the previous question it does not go underneath the negative reward block. Doing more iterations could lead to it finding the path or increase the exploration a bit.

## Environment B (the effect of epsilon and gamma)

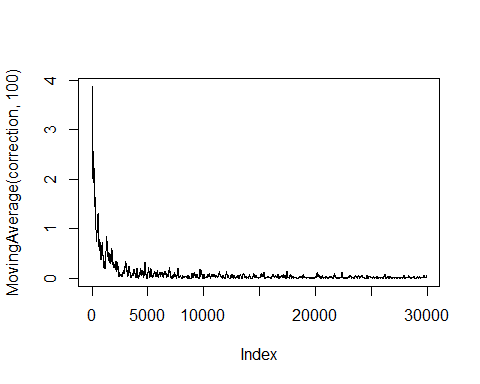
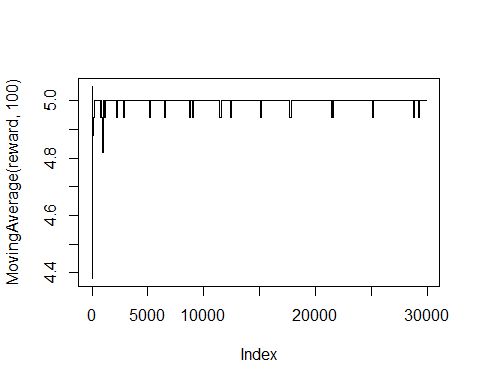
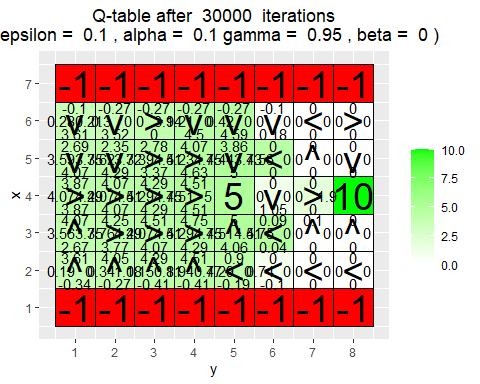
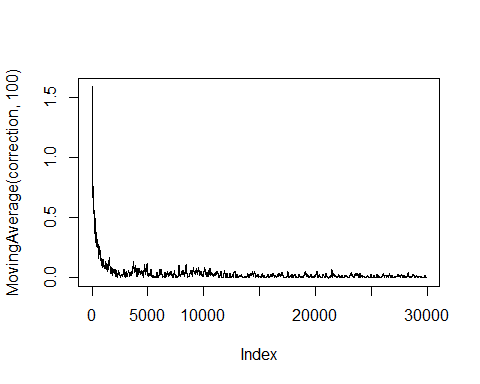
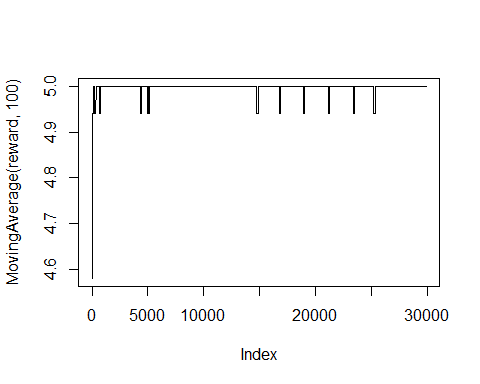
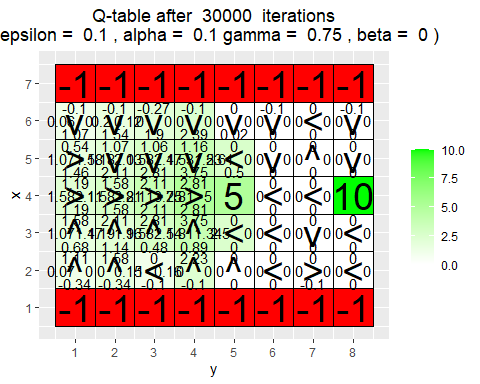
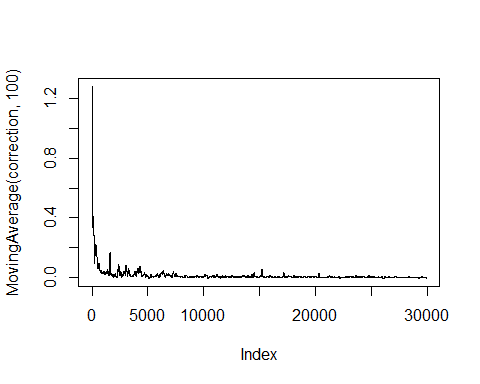
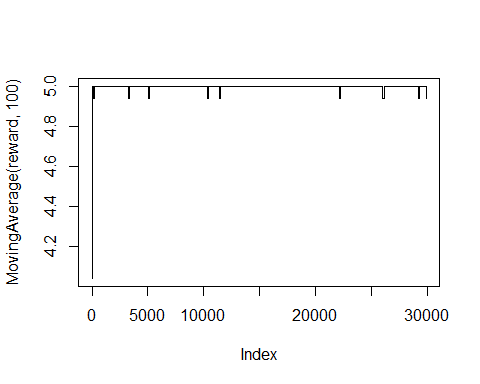
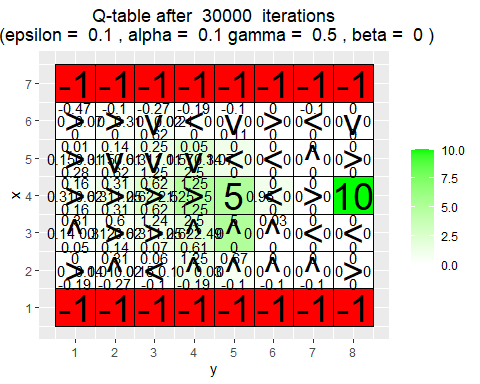
H <- 7  
W <- 8  
  
reward\_map <- matrix(0, nrow = H, ncol = W)  
reward\_map[1,] <- -1  
reward\_map[7,] <- -1  
reward\_map[4,5] <- 5  
reward\_map[4,8] <- 10  
  
q\_table <- array(0,dim = c(H,W,4))  
  
vis\_environment()



MovingAverage <- function(x, n){  
   
 cx <- c(0,cumsum(x))  
 rsum <- (cx[(n+1):length(cx)] - cx[1:(length(cx) - n)]) / n  
   
 return (rsum)  
}  
  
for(j in c(0.5,0.75,0.95)){  
 q\_table <- array(0,dim = c(H,W,4))  
 reward <- NULL  
 correction <- NULL  
   
 for(i in 1:30000){  
 foo <- q\_learning(gamma = j, start\_state = c(4,1))  
 reward <- c(reward,foo[1])  
 correction <- c(correction,foo[2])  
 }  
   
 vis\_environment(i, gamma = j)  
 plot(MovingAverage(reward,100),type = "l")  
 plot(MovingAverage(correction,100),type = "l")  
}



for(j in c(0.5,0.75,0.95)){  
 q\_table <- array(0,dim = c(H,W,4))  
 reward <- NULL  
 correction <- NULL  
   
 for(i in 1:30000){  
 foo <- q\_learning(epsilon = 0.1, gamma = j, start\_state = c(4,1))  
 reward <- c(reward,foo[1])  
 correction <- c(correction,foo[2])  
 }  
   
 vis\_environment(i, epsilon = 0.1, gamma = j)  
 plot(MovingAverage(reward,100),type = "l")  
 plot(MovingAverage(correction,100),type = "l")  
}

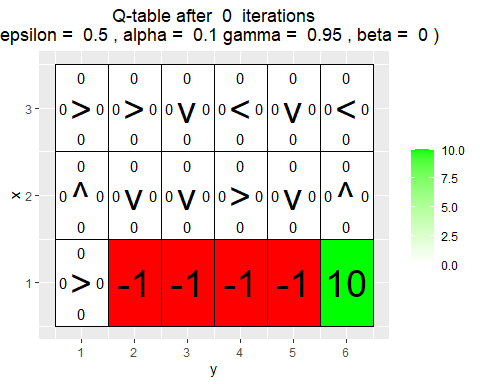


When increasing the value for we increase the value of future rewards for the agent. With an increased we have increased chance of exploration, would give a 50-50 chance of the agent exploring vs exploiting the current best reward.

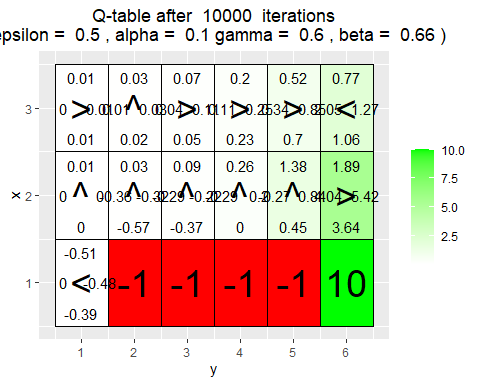
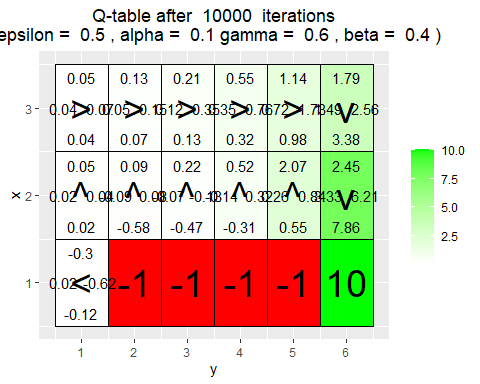
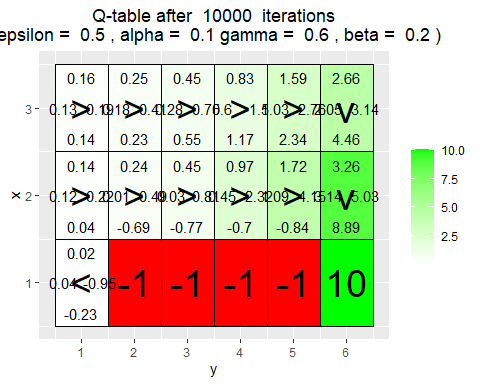
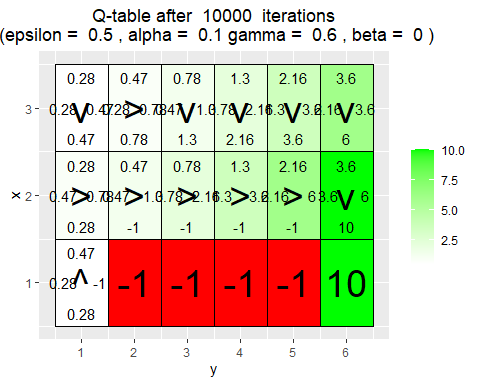
We want a good mix of these two variables to not get stuck in states were rewards are “good enough” or take unnecessary paths.

## Environment C (the effect of beta).

H <- 3  
W <- 6  
  
reward\_map <- matrix(0, nrow = H, ncol = W)  
reward\_map[1,2:5] <- -1  
reward\_map[1,6] <- 10  
  
q\_table <- array(0,dim = c(H,W,4))  
  
vis\_environment()



for(j in c(0,0.2,0.4,0.66)){  
 q\_table <- array(0,dim = c(H,W,4))  
   
 for(i in 1:10000)  
 foo <- q\_learning(gamma = 0.6, beta = j, start\_state = c(1,1))  
   
 vis\_environment(i, gamma = 0.6, beta = j)  
}



is the slipping factor and it can make the agent slip left or right with equal probability from the state it wanted to go to. In the figures we can see that a higher makes it less likely to slip into the negative rewards. It has done this by avoiding to go to the states close to the negative reward block